## LOYOLA COLLEGE (AUTONOMOUS), CHENNAI - 600034

B.Sc. DEGREE EXAMINATION - MATHEMATICS

FIFTH SEMESTER - APRIL 2013
MT 5507/MT 5504-OPERATIONS RESEARCH

Date: 11/05/2013
Dept. No. $\square$ Max. : 100 Marks
Time: 9:00-12:00

## PART - A

ANSWER ALL QUESTIONS:

1. Define surplus variables.
2. Define a optimum basic feasible solution.
3. What is a transportation problem?
4. Give the mathematical formulation of an assignment problem.
5. Define payoff matrix.
6. Define saddle point.
7. Define a dummy activity.
8. State any two rules to be followed while constructing a network.
9. Define the following terms i) Lead time ii) Planning Horizon.
10.What is Economic Order Quantity?

## PART-B

ANSWER ANY FIVE QUESTIONS:
11. Use the graphical method to solve the following LP problem.

Maximize $Z=3 x_{1}+2 x_{2}$
Subjectto $-2 x_{1}+x_{2} \leq 1$

$$
x_{1} \leq 2
$$

$x_{1}+x_{2} \leq$ and $x_{1}, x_{2} \geq 0$
12. Use dual simplex method to solve the LP problem

Minimize $3 x_{1}+x_{2}$ subject to the constraints

$$
\begin{aligned}
& x_{1}+x_{2} \geq 1 \\
& 2 x_{1}+3 x_{2} \geq 2 \quad \text { and } \\
& x_{1}, x_{2} \geq 0 .
\end{aligned}
$$

13. A department has five employees with five jobs to be performed. The time (in hours) each man will take to perform each job is given in the effectiveness matrix.

## Employees

|  |  | $I$ | $I I$ | $I I I$ | $I V$ | $V$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $A$ | 10 | 5 | 13 | 15 | 16 |
|  | $B$ | 3 | 9 | 18 | 13 | 6 |
| Jobs | $C$ | 10 | 7 | 2 | 2 | 2 |
|  | $D$ | 7 | 11 | 9 | 7 | 12 |
|  | $E$ | 7 | 9 | 10 | 4 | 12 |

How should the jobs be allocated, one per employee, so as to minimize the total man - hours?
14. Use graphical method in solving the following game and find the value of the game.

Player B
Player A $\begin{gathered} \\ \mathrm{A}_{1}\end{gathered}\left(\begin{array}{cccc}\mathrm{B}_{1} & \mathrm{~B}_{2} & \mathrm{~B}_{3} & \mathrm{~B}_{4} \\ 2 & 2 & 3 & -2 \\ 4 & 3 & 2 & 6\end{array}\right)$
15. In a game of matching coins with two players, suppose A wins one unit of value when there are two heads, wins nothing when there are two tails and losses $1 / 2$ unit of value when there is one head and one tail. Determine the payoff matrix, the best strategies for each player and the value of the game.
16. A Television cable company is in the process of providing cable service to five new housing development areas. The following figure depicts the potential TV linkages among the five areas. The cable miles are shown on each branch. Determine the most economical cable network.

17. Determine the maximal flow in the following network.

18. The annual demand of a product is 10,000 units. Each unit costs Rs 100 if orders placed in quantities below 200 units but for orders of 200 or above the price is Rs 95. The annual inventory holding costs is 10 per cent of the value of the item and the ordering cost is Rs 5 per order. Find the economic lot size.(4+4)

## PART - C

## ANSWER ANY TWO QUESTIONS:

19. Use the simplex method to solve the following LP problem.

Maximize $Z=3 x_{1}+5 x_{2}+4 x_{3}$ subject to the constraints

$$
\begin{aligned}
& 2 x_{1}+3 x_{2} \leq 8 \\
& 2 x_{2}+5 x_{3} \leq 10 \\
& 3 x_{1}+2 x_{2}+4 x_{3} \leq 15 \\
& x_{1}, x_{2}, x_{3} \geq 0
\end{aligned}
$$

20. Find the optimal solution for the following transportation problem using MODI method.

|  | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ | $\mathrm{D}_{4}$ | Supply |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{S}_{1}$ | 19 | 30 | 50 | 10 | 7 |
| $\mathrm{~S}_{2}$ | 70 | 30 | 40 | 60 | 9 |
| $\mathrm{~S}_{3}$ | 40 | 8 | 70 | 20 | 18 |
| Demand | 5 | 8 | 7 | 14 | 34 |

21. a) The daily milk production (in million litres) at each plant of a dairy firm having three plants $P_{1}, P_{2}$ and $P_{3}$ are 6,1 and 10 respectively. The firm must fulfil the needs of its four distribution centres. The minimum requirements at each centre (in million litres) are $7,5,3$ and 2 respectively. The cost of shipping one million litres from each plant to each distribution centre is given in the following table in hundreds of rupees:

Distribution centre

|  |  | $D_{1}$ | $D_{2}$ | $D_{3}$ | $D_{4}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $P_{1}$ | 2 | 3 | 11 | 7 |
| Plant | $P_{2}$ | 1 | 0 | 6 | 1 |
|  | $P_{3}$ | 5 | 8 | 15 | 9 |

Find its initial basic feasible solution by i) Least cost method ii) Vogel's Approximation method.
b) Solve the game whose payoff matrix is given below by the principles of dominance:

Player B

|  |
| :---: |
|  |
| Player A |
|  |  |
|  |  |
|  |
|  |
|  |
| $\mathrm{~A}_{4}$ |\(\left[\begin{array}{cccc}3 \& \mathrm{~B}_{2} \& \mathrm{~B}_{3} \& \mathrm{~B}_{4} <br>

3 \& 4 \& 4 \& 0 <br>
4 \& 2 \& 4 \& 4 <br>
0 \& 4 \& 0 \& 8\end{array}\right)\)
22. a) Determine the shortest routes between the source node and every other node in the following network using Dijkstra's algorithm
(Source)

b) b) Determine the critical path and compute the floats for the noncritical activities of the project network given below:

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